

MATH LOVE INSTITUTE

CBSE Class 9 Mathematics (Code: 041)

Sample Paper 1 - Home Exam 2025-26 with Complete Solutions

Based on Latest CBSE Syllabus & Exam Pattern 2025-26

Maximum Marks	80 (Theory)
Time Allowed	3 Hours
Class	IX (Nine)
Subject	Mathematics (041)

GENERAL INSTRUCTIONS:

1. This question paper contains **38 questions** divided into **Five Sections A, B, C, D and E**.
2. **Section A:** 20 MCQs of 1 mark each (20 marks)
3. **Section B:** 5 Very Short Answer Type questions of 2 marks each (10 marks)
4. **Section C:** 6 Short Answer Type questions of 3 marks each (18 marks)
5. **Section D:** 4 Long Answer Type questions of 5 marks each (20 marks)
6. **Section E:** 3 Case Study Based questions of 4 marks each (12 marks)
7. All questions are **compulsory**. However, internal choices have been provided in some questions.
8. Draw neat diagrams wherever required. Take $\pi = 22/7$ wherever required.
9. Use of calculators is **NOT** permitted.

© 2025 MATH LOVE INSTITUTE - QUESTION PAPER

SECTION A - MULTIPLE CHOICE QUESTIONS (1 × 20 = 20 Marks)

Q1. Which of the following is an irrational number? [1]

- (a) $\sqrt{4}$
- (b) $\sqrt{9}$
- (c) $\sqrt{7}$
- (d) $\sqrt{16}$

Q2. The value of $(2 + \sqrt{3})(2 - \sqrt{3})$ is: [1]

- (a) 1
- (b) 4
- (c) 7
- (d) $1 - \sqrt{3}$

Q3. The degree of the polynomial $5x^3 - 4x^2 + 7x - 8$ is: [1]

- (a) 1
- (b) 2
- (c) 3
- (d) 4

Q4. The graph of the linear equation $y = 3$ is a line: [1]

- (a) Parallel to x-axis
- (b) Parallel to y-axis
- (c) Passing through origin
- (d) Passing through (0, 3) and (1, 3)

Q5. If the point (3, 4) lies on the graph of $3y = ax + 7$, then the value of a is: [1]

- (a) $4/3$
- (b) $5/3$
- (c) 1
- (d) $7/3$

MATH LOVE INSTITUTE - QUESTION PAPER

Q6. In $\triangle ABC$, if $\angle A = 50^\circ$ and $\angle B = 60^\circ$, then $\angle C$ is: [1]

- (a) 50°
- (b) 60°
- (c) 70°
- (d) 80°

Q7. If two sides of a triangle are equal, the angles opposite to them are: [1]

- (a) Equal
- (b) Unequal
- (c) Supplementary
- (d) Complementary

Q8. The sum of all angles of a quadrilateral is: [1]

- (a) 180°
- (b) 270°
- (c) 360°
- (d) 450°

Q9. A diagonal of a rectangle is 17 cm and its width is 8 cm. The area of the rectangle is: [1]

- (a) 120 cm^2
- (b) 136 cm^2
- (c) 150 cm^2
- (d) 170 cm^2

Q10. The radius of a circle is 7 cm. The circumference of the circle is: [1]

- (a) 22 cm
- (b) 44 cm
- (c) 154 cm
- (d) 308 cm

© 2025 MATH LOVE INSTITUTE - QUESTION PAPER

Q11. A chord of a circle of radius 10 cm subtends a right angle at its centre. The length of [1]
the chord is:

- (a) $5\sqrt{2}$ cm
- (b) 10 cm
- (c) $10\sqrt{2}$ cm
- (d) 20 cm

Q12. The semi-perimeter of a triangle with sides 12 cm, 16 cm and 20 cm is: [1]

- (a) 24 cm
- (b) 32 cm
- (c) 48 cm
- (d) 96 cm

Q13. The total surface area of a cube with edge 10 cm is: [1]
(a) 100 cm^2
(b) 400 cm^2
(c) 600 cm^2
(d) 1000 cm^2

Q14. The volume of a cuboid with dimensions $5 \text{ cm} \times 4 \text{ cm} \times 3 \text{ cm}$ is: [1]
(a) 12 cm^3
(b) 20 cm^3
(c) 60 cm^3
(d) 80 cm^3

Q15. If the diameter of a hemisphere is 14 cm, its total surface area is: [1]
(a) 154 cm^2
(b) 231 cm^2
(c) 308 cm^2
(d) 462 cm^2

MATH LOVE INSTITUTE - QUESTION PAPER

Q16. The class mark of the class 120-150 is: [1]
(a) 120
(b) 130
(c) 135
(d) 140

Q17. The mean of first five natural numbers is: [1]
(a) 2
(b) 2.5
(c) 3
(d) 3.5

Q18. If the coordinates of two points are $P(0, 6)$ and $Q(0, -2)$, then (abscissa of P) - (abscissa of Q) is: [1]
(a) 8
(b) 4
(c) 2
(d) 0

- Q19.** The point $(-3, 5)$ lies in the quadrant: [1]
- (a) I
 - (b) II
 - (c) III
 - (d) IV

- Q20.** If $x + 2y = 5$ and $3x - 2y = 11$, then x is equal to: [1]
- (a) 2
 - (b) 3
 - (c) 4
 - (d) 5

© 2025 MATH LOVE INSTITUTE - QUESTION PAPER

SECTION B - VERY SHORT ANSWER TYPE QUESTIONS ($2 \times 5 = 10$ Marks)

- Q21.** Express $0.\overline{6}$ ($0.666\dots$) in the form of p/q where p and q are integers and $q \neq 0$. [2]
- Q22.** Find the value of k , if $x = 1$ and $y = 2$ is a solution of the equation $2x + 3y = k$. [2]
- Q23.** In the figure, if $AB \parallel CD$, $\angle APQ = 50^\circ$ and $\angle PRD = 130^\circ$, find $\angle QPR$. [2]
[Assume a figure showing two parallel lines with transversal]
- Q24.** If the area of an equilateral triangle is $16\sqrt{3} \text{ cm}^2$, find its perimeter. [2]
- Q25.** Find the mode of the following data: 12, 14, 12, 16, 15, 13, 14, 18, 19, 12, 14, 15, 16, 15, 16, 16, 15, 17, 13, 16. [2]

MATH LOVE INSTITUTE - QUESTION PAPER

SECTION C - SHORT ANSWER TYPE QUESTIONS ($3 \times 6 = 18$ Marks)

- Q26.** Rationalize the denominator: $1/(\sqrt{7} - \sqrt{6})$ [3]
- Q27.** If $x + y = 12$ and $xy = 32$, find the value of $x^3 + y^3$. [3]
- Q28.** The angles of a quadrilateral are in the ratio 3:4:5:6. Find all the angles of the quadrilateral. [3]

Q29. In $\triangle ABC$, $AB = AC$ and $\angle A = 80^\circ$. Find $\angle B$ and $\angle C$. [3]

OR

Show that the angles of an equilateral triangle are 60° each.

Q30. Find the area of a triangle whose sides are 18 cm, 24 cm and 30 cm using Heron's formula. [3]

Q31. A hemispherical bowl of internal radius 9 cm is full of liquid. The liquid is to be filled in cylindrical bottles of radius 3 cm and height 4 cm. How many bottles are required? [3]

© 2025 MATH LOVE INSTITUTE - QUESTION PAPER

SECTION D - LONG ANSWER TYPE QUESTIONS (5 × 4 = 20 Marks)

Q32. Prove that: $(\sqrt{3} + \sqrt{5})^2 = 8 + 2\sqrt{15}$. Hence find the value of $1/(8 + 2\sqrt{15})$ after rationalizing the denominator. [5]

OR

If $x = 2 + \sqrt{3}$, find the value of $x^3 + 1/x^3$.

Q33. Factorise: $x^3 + 13x^2 + 32x + 20$ [5]

Q34. In $\triangle ABC$, D, E and F are respectively the mid-points of sides BC, CA and AB. Show that $\triangle ABC$ is divided into four congruent triangles by joining D, E and F. [5]

OR

In a triangle, if square of one side is equal to the sum of the squares of the other two sides, prove that the angle opposite the first side is a right angle. (Pythagoras Theorem - Converse)

Q35. Draw the graph of the linear equation $3x + 4y = 12$. From the graph, find: [5]

- (i) The coordinates where the line meets X-axis
- (ii) The coordinates where the line meets Y-axis
- (iii) The coordinates of one more point on the line

MATH LOVE INSTITUTE - QUESTION PAPER

SECTION E - CASE STUDY BASED QUESTIONS (4 × 3 = 12 Marks)

Q36.

[4]

CASE STUDY 1: School Garden Design

A school wants to design a triangular garden with dimensions as follows: The three sides of the triangular garden are 26 m, 28 m and 30 m. The school management wants to plant grass in the garden and also construct a fountain at the centroid of the triangle.

Based on the above information, answer the following questions:

- (i) Find the semi-perimeter of the triangular garden. [1 mark]
- (ii) Find the area of the triangular garden using Heron's formula. [2 marks]
- (iii) If the cost of planting grass is ₹15 per m^2 , find the total cost of planting grass in the entire garden. [1 mark]

Q37.

[4]

CASE STUDY 2: Water Tank Problem

A cylindrical water tank has radius 1.4 m and height 2 m. The water from this tank is to be transferred to smaller cylindrical containers having radius 0.7 m and height 0.5 m.

Based on the above information, answer the following questions:

- (i) Find the volume of the large water tank. [1 mark]
- (ii) Find the volume of one small container. [1 mark]
- (iii) How many small containers are required to empty the large tank completely? [2 marks]

CASE STUDY 3: Temperature Analysis

The following data shows the daily maximum temperatures (in °C) recorded in a city for 30 days:

Temperature (°C)	25-30	30-35	35-40	40-45
Number of days	4	8	12	6

Based on the above information, answer the following questions:

(i) What is the class width of the distribution? **[1 mark]**

(ii) Write the class mark of the class 35-40. **[1 mark]**

(iii) Calculate the mean temperature using the formula:

Mean = $\frac{\sum(f_i \times x_i)}{\sum f_i}$, where x_i is the class mark and f_i is the frequency. **[2 marks]**

 **END OF QUESTION PAPER** 

Total Marks: 80

Section A: 20 marks | Section B: 10 marks | Section C: 18 marks

Section D: 20 marks | Section E: 12 marks

Based on CBSE Class 9 Mathematics Syllabus 2025-26

Most Expected Questions for Home Exams

 **DETAILED SOLUTIONS WITH STEP-BY-STEP EXPLANATIONS**

SECTION A - SOLUTIONS (1 × 20 = 20 Marks)

Q1. Answer: (c) $\sqrt{7}$

Explanation: $\sqrt{4} = 2$, $\sqrt{9} = 3$, $\sqrt{16} = 4$ (all rational numbers). $\sqrt{7}$ cannot be expressed as p/q form, hence it is irrational.

Q2. Answer: (a) 1

Solution:

$$(2 + \sqrt{3})(2 - \sqrt{3}) = 2^2 - (\sqrt{3})^2 \text{ [Using } (a+b)(a-b) = a^2 - b^2\text{]} \\ = 4 - 3 = 1$$

Q3. Answer: (c) 3

Explanation: The degree of a polynomial is the highest power of the variable. Here, the highest power of x is 3.

Q4. Answer: (a) Parallel to x-axis

Explanation: $y = 3$ means for all values of x, y remains constant at 3. This represents a horizontal line parallel to x-axis passing through (0, 3).

Q5. Answer: (b) $\frac{5}{3}$

Solution:

Point (3, 4) lies on $3y = ax + 7$

Substituting $x = 3, y = 4$:

$$3(4) = a(3) + 7$$

$$12 = 3a + 7$$

$$3a = 5$$

$$a = 5/3$$

MATH LOVE INSTITUTE - SOLUTIONS

Q6. Answer: (c) 70° **Solution:**

In $\triangle ABC$, $\angle A + \angle B + \angle C = 180^\circ$ [Angle sum property]

$$50^\circ + 60^\circ + \angle C = 180^\circ$$

$$\angle C = 180^\circ - 110^\circ = 70^\circ$$

Q7. Answer: (a) Equal

Explanation: This is the Isosceles Triangle Theorem - angles opposite to equal sides are equal.

Q8. Answer: (c) 360°

Explanation: The sum of all interior angles of a quadrilateral is 360° .

Q9. Answer: (a) 120 cm^2 **Solution:**

In rectangle, $\text{diagonal}^2 = \text{length}^2 + \text{width}^2$

$$17^2 = l^2 + 8^2$$

$$289 = l^2 + 64$$

$$l^2 = 225$$

$$l = 15 \text{ cm}$$

$$\text{Area} = l \times w = 15 \times 8 = 120 \text{ cm}^2$$

Q10. Answer: (b) 44 cm

Solution:

$$\text{Circumference} = 2\pi r = 2 \times (22/7) \times 7 = 44 \text{ cm}$$

© 2025 MATH LOVE INSTITUTE - SOLUTIONS

Q11. Answer: (c) $10\sqrt{2}$ cm

Solution:

Since chord subtends 90° at center, triangle formed is right-angled isosceles

Using Pythagoras: $\text{Chord}^2 = r^2 + r^2$

$$\text{Chord}^2 = 10^2 + 10^2 = 200$$

$$\text{Chord} = \sqrt{200} = 10\sqrt{2} \text{ cm}$$

Q12. Answer: (a) 24 cm

Solution:

Semi-perimeter, $s = (a + b + c)/2$

$$s = (12 + 16 + 20)/2 = 48/2 = 24 \text{ cm}$$

Q13. Answer: (c) 600 cm^2

Solution:

Total Surface Area of cube = $6a^2$

$$= 6 \times 10^2 = 6 \times 100 = 600 \text{ cm}^2$$

Q14. Answer: (c) 60 cm^3

Solution:

$$\begin{aligned}\text{Volume of cuboid} &= l \times b \times h \\ &= 5 \times 4 \times 3 = 60 \text{ cm}^3\end{aligned}$$

Q15. Answer: (d) 462 cm²

Solution:

$$\text{Radius} = d/2 = 14/2 = 7 \text{ cm}$$

$$\begin{aligned}\text{Total Surface Area of hemisphere} &= 3\pi r^2 \\ &= 3 \times (22/7) \times 7 \times 7 \\ &= 3 \times 22 \times 7 = 462 \text{ cm}^2\end{aligned}$$

MATH LOVE INSTITUTE - SOLUTIONS

Q16. Answer: (c) 135

Solution:

$$\begin{aligned}\text{Class mark} &= (\text{Upper limit} + \text{Lower limit})/2 \\ &= (150 + 120)/2 = 270/2 = 135\end{aligned}$$

Q17. Answer: (c) 3

Solution:

$$\begin{aligned}\text{First five natural numbers: } &1, 2, 3, 4, 5 \\ \text{Mean} &= (1 + 2 + 3 + 4 + 5)/5 = 15/5 = 3\end{aligned}$$

Q18. Answer: (d) 0

Solution:

$$\begin{aligned}\text{Abcissa of P} &= 0, \text{ Abcissa of Q} = 0 \\ \text{Difference} &= 0 - 0 = 0\end{aligned}$$

Q19. Answer: (b) II

Explanation: Point $(-3, 5)$ has negative x-coordinate and positive y-coordinate, hence it lies in Quadrant II.

Q20. Answer: (c) 4

Solution:

$$x + 2y = 5 \dots(i)$$

$$3x - 2y = 11 \dots(ii)$$

Adding (i) and (ii):

$$4x = 16$$

$$x = 4$$

© 2025 MATH LOVE INSTITUTE - SOLUTIONS

SECTION B - SOLUTIONS ($2 \times 5 = 10$ Marks)

Q21. Solution:

Marking Scheme: 1 mark for method + 1 mark for answer

Let $x = 0.666\dots$

Then $10x = 6.666\dots$

Subtracting: $10x - x = 6.666\dots - 0.666\dots$

$$9x = 6$$

$$x = 6/9 = 2/3$$

Answer: $0.\overline{6} = 2/3$

Q22. Solution:

Marking Scheme: 1 mark for substitution + 1 mark for value of k

Given equation: $2x + 3y = k$

Substituting $x = 1, y = 2$:

$$2(1) + 3(2) = k$$

$$2 + 6 = k$$

$$k = 8$$

Q23. Solution:

Marking Scheme: 1 mark for identifying angles + 1 mark for calculation

Since $AB \parallel CD$ and PQ is a transversal:

$$\angle APQ + \angle PQR = 180^\circ \text{ [Co-interior angles]}$$

$$50^\circ + \angle PQR = 180^\circ$$

$$\angle PQR = 130^\circ$$

$$\angle PRD = 130^\circ \text{ (given)}$$

$$\angle PQR + \angle QPR + \angle PRQ = 180^\circ \text{ [Triangle angle sum]}$$

Since $\angle PQR$ and $\angle PRD$ are alternate interior angles:

$$\angle QPR = 180^\circ - 130^\circ - \angle PQR$$

$$\angle QPR = 80^\circ$$

Q24. Solution:

Marking Scheme: 1 mark for finding side + 1 mark for perimeter

$$\text{Area of equilateral triangle} = (\sqrt{3}/4)a^2$$

$$16\sqrt{3} = (\sqrt{3}/4)a^2$$

$$a^2 = 64$$

$$a = 8 \text{ cm}$$

$$\text{Perimeter} = 3a = 3 \times 8 = \mathbf{24 \text{ cm}}$$

Q25. Solution:

Marking Scheme: 1 mark for frequency table + 1 mark for mode

Frequency count:

12 appears 3 times

13 appears 2 times

14 appears 3 times

15 appears 4 times

16 appears 5 times

17 appears 1 time

18 appears 1 time

19 appears 1 time

Mode = 16 (highest frequency)

MATH LOVE INSTITUTE - SOLUTIONS

SECTION C - SOLUTIONS (3 × 6 = 18 Marks)

Q26. Solution:

Marking Scheme: 1 mark for multiplying conjugate + 1 mark for simplification + 1 mark for final answer

$$1/(\sqrt{7} - \sqrt{6})$$

Multiplying numerator and denominator by $(\sqrt{7} + \sqrt{6})$:

$$= [1 \times (\sqrt{7} + \sqrt{6})] / [(\sqrt{7} - \sqrt{6})(\sqrt{7} + \sqrt{6})]$$

$$= (\sqrt{7} + \sqrt{6}) / [(\sqrt{7})^2 - (\sqrt{6})^2]$$

$$= (\sqrt{7} + \sqrt{6}) / (7 - 6)$$

$$= (\sqrt{7} + \sqrt{6}) / 1$$

$$= \sqrt{7} + \sqrt{6}$$

Q27. Solution:

Marking Scheme: 1 mark for formula + 1 mark for calculation + 1 mark for final answer

Given: $x + y = 12$, $xy = 32$

Using identity: $x^3 + y^3 = (x + y)^3 - 3xy(x + y)$

$$x^3 + y^3 = (12)^3 - 3(32)(12)$$

$$= 1728 - 1152$$

$$= \mathbf{576}$$

Q28. Solution:

Marking Scheme: 1 mark for setting up equation + 1 mark for finding x + 1 mark for all angles

Let the angles be $3x$, $4x$, $5x$, and $6x$

Sum of angles of quadrilateral = 360°

$$3x + 4x + 5x + 6x = 360^\circ$$

$$18x = 360^\circ$$

$$x = 20^\circ$$

Angles are:

$$3x = 3(20^\circ) = 60^\circ$$

$$4x = 4(20^\circ) = 80^\circ$$

$$5x = 5(20^\circ) = 100^\circ$$

$$6x = 6(20^\circ) = 120^\circ$$

Q29. Solution:

Marking Scheme: 1 mark for using isosceles property + 1 mark for angle sum + 1 mark for answer

Given: $AB = AC$ (isosceles triangle)

$$\angle A = 80^\circ$$

Since $AB = AC$, $\angle B = \angle C$ [Angles opposite to equal sides are equal]

Using angle sum property:

$$\angle A + \angle B + \angle C = 180^\circ$$

$$80^\circ + \angle B + \angle B = 180^\circ \text{ [Since } \angle B = \angle C \text{]}$$

$$80^\circ + 2\angle B = 180^\circ$$

$$2\angle B = 100^\circ$$

$$\angle B = 50^\circ$$

$$\angle B = 50^\circ \text{ and } \angle C = 50^\circ$$

OR

In equilateral triangle: $AB = BC = CA$

Since $AB = BC$, $\angle A = \angle C$ [Angles opposite to equal sides]

Since $BC = CA$, $\angle A = \angle B$ [Angles opposite to equal sides]

Therefore, $\angle A = \angle B = \angle C$

Let each angle = x

$$x + x + x = 180^\circ \text{ [Angle sum property]}$$

$$3x = 180^\circ$$

$$x = 60^\circ$$

Hence, each angle of an equilateral triangle is 60° .

Q30. Solution:

Marking Scheme: 1 mark for semi-perimeter + 1 mark for Heron's formula + 1 mark for calculation

Given: $a = 18 \text{ cm}$, $b = 24 \text{ cm}$, $c = 30 \text{ cm}$

Semi-perimeter, $s = (a + b + c)/2$

$$s = (18 + 24 + 30)/2 = 72/2 = 36 \text{ cm}$$

Using Heron's formula:

$$\text{Area} = \sqrt{[s(s-a)(s-b)(s-c)]}$$

$$= \sqrt{[36(36-18)(36-24)(36-30)]}$$

$$= \sqrt{[36 \times 18 \times 12 \times 6]}$$

$$= \sqrt{[46656]}$$

$$= 216 \text{ cm}^2$$

Area = 216 cm²

Q31. Solution:

Marking Scheme: 1 mark for hemisphere volume + 1 mark for cylinder volume + 1 mark for number of bottles

Volume of hemispherical bowl = $(2/3)\pi r^3$

$$= (2/3) \times (22/7) \times 9^3$$

$$= (2/3) \times (22/7) \times 729$$

$$= 1527.43 \text{ cm}^3 \text{ (approx)}$$

Volume of one cylindrical bottle = $\pi r^2 h$

$$= (22/7) \times 3^2 \times 4$$

$$= (22/7) \times 9 \times 4$$

$$= 113.14 \text{ cm}^3 \text{ (approx)}$$

Number of bottles = Volume of bowl / Volume of one bottle

$$= 1527.43 / 113.14$$

$$\approx 13.5$$

Therefore, 14 bottles are required

SECTION D - SOLUTIONS (5 × 4 = 20 Marks)

Q32. Solution:

Marking Scheme: 2 marks for proving + 2 marks for rationalization + 1 mark for final answer

To Prove: $(\sqrt{3} + \sqrt{5})^2 = 8 + 2\sqrt{15}$

$$\begin{aligned} \text{LHS} &= (\sqrt{3} + \sqrt{5})^2 \\ &= (\sqrt{3})^2 + 2(\sqrt{3})(\sqrt{5}) + (\sqrt{5})^2 \text{ [Using } (a+b)^2 = a^2 + 2ab + b^2\text{]} \\ &= 3 + 2\sqrt{15} + 5 \\ &= 8 + 2\sqrt{15} = \text{RHS} \end{aligned}$$

Hence Proved

Now, $1/(8 + 2\sqrt{15})$

Multiplying numerator and denominator by $(8 - 2\sqrt{15})$:

$$\begin{aligned} &= (8 - 2\sqrt{15}) / [(8 + 2\sqrt{15})(8 - 2\sqrt{15})] \\ &= (8 - 2\sqrt{15}) / [64 - 4(15)] \\ &= (8 - 2\sqrt{15}) / (64 - 60) \\ &= (8 - 2\sqrt{15}) / 4 \\ &= 2 - (\sqrt{15}/2) \end{aligned}$$

OR

Given: $x = 2 + \sqrt{3}$

$$1/x = 1/(2 + \sqrt{3}) = (2 - \sqrt{3})/[(2 + \sqrt{3})(2 - \sqrt{3})] = (2 - \sqrt{3})/(4 - 3) = 2 - \sqrt{3}$$

$$\text{Now, } x + 1/x = (2 + \sqrt{3}) + (2 - \sqrt{3}) = 4$$

We need $x^3 + 1/x^3$

Using identity: $x^3 + 1/x^3 = (x + 1/x)^3 - 3(x + 1/x)$

$$= (4)^3 - 3(4)$$

$$= 64 - 12$$

$$= \mathbf{52}$$

Q33. Solution:

Marking Scheme: 2 marks for finding factor + 2 marks for factorization + 1 mark for final answer

Let $p(x) = x^3 + 13x^2 + 32x + 20$

By trial, $p(-1) = (-1)^3 + 13(-1)^2 + 32(-1) + 20$

$$= -1 + 13 - 32 + 20 = 0$$

So, $(x + 1)$ is a factor

Dividing $p(x)$ by $(x + 1)$:

$$x^3 + 13x^2 + 32x + 20 = (x + 1)(x^2 + 12x + 20)$$

Now factorizing $x^2 + 12x + 20$:

$$= x^2 + 10x + 2x + 20$$

$$= x(x + 10) + 2(x + 10)$$

$$= (x + 2)(x + 10)$$

Therefore: $x^3 + 13x^2 + 32x + 20 = (x + 1)(x + 2)(x + 10)$

Q34. Solution:

Marking Scheme: 2 marks for showing congruence + 2 marks for proving all four triangles congruent + 1 mark for conclusion

Given: In $\triangle ABC$, D, E, F are midpoints of BC, CA, AB respectively

To Prove: $\triangle ABC$ is divided into four congruent triangles

Proof:

By Midpoint Theorem:

- $EF \parallel BC$ and $EF = (1/2)BC = BD = DC$
- $FD \parallel AC$ and $FD = (1/2)AC = AE = EC$
- $DE \parallel AB$ and $DE = (1/2)AB = AF = FB$

Now, $BDEF$ is a parallelogram ($EF \parallel BD$ and $EF = BD$)

Similarly, $AFDE$ and $FDCE$ are parallelograms

In $\triangle FBD$ and $\triangle DEF$:

$FB = DE$ (proved above)

$BD = EF$ (proved above)

$FD = FD$ (common)

$\therefore \triangle FBD \cong \triangle DEF$ (SSS congruence)

Similarly, we can prove:

$\triangle AEF \cong \triangle DEF$ and $\triangle CDE \cong \triangle DEF$

Therefore, $\triangle ABC$ is divided into four congruent triangles.

OR

Pythagoras Theorem (Converse):

Statement: In a triangle, if square of one side equals the sum of squares of the other two sides, then the angle opposite the first side is a right angle.

Given: In $\triangle ABC$, $AC^2 = AB^2 + BC^2$

To Prove: $\angle B = 90^\circ$

Construction: Draw $\triangle PQR$ such that $PQ = AB$, $QR = BC$ and $\angle Q = 90^\circ$

Proof:

In $\triangle PQR$, $\angle Q = 90^\circ$

By Pythagoras theorem:

$$PR^2 = PQ^2 + QR^2$$

$$PR^2 = AB^2 + BC^2 \dots(i) \text{ [Since } PQ = AB, QR = BC]$$

$$\text{But given: } AC^2 = AB^2 + BC^2 \dots(ii)$$

From (i) and (ii):

$$PR^2 = AC^2$$

$$\therefore PR = AC$$

Now in $\triangle ABC$ and $\triangle PQR$:

$$AB = PQ \text{ (by construction)}$$

$$BC = QR \text{ (by construction)}$$

$$AC = PR \text{ (proved)}$$

$$\therefore \triangle ABC \cong \triangle PQR \text{ (SSS congruence)}$$

$$\therefore \angle B = \angle Q = 90^\circ \text{ (Corresponding parts of congruent triangles)}$$

Hence Proved

Q35. Solution:

Marking Scheme: 2 marks for finding points + 2 marks for graph + 1 mark for coordinates

$$\text{Given equation: } 3x + 4y = 12$$

Finding points:

$$\text{When } x = 0: 3(0) + 4y = 12 \rightarrow y = 3, \text{ Point: } (0, 3)$$

$$\text{When } y = 0: 3x + 4(0) = 12 \rightarrow x = 4, \text{ Point: } (4, 0)$$

$$\text{When } x = 4: 3(4) + 4y = 12 \rightarrow y = 0, \text{ Point: } (4, 0)$$

$$\text{When } x = -4: 3(-4) + 4y = 12 \rightarrow 4y = 24 \rightarrow y = 6, \text{ Point: } (-4, 6)$$

Table of values:

x	0	4	-4
---	---	---	----

y	3	0	6
---	---	---	---

[Students should plot these points on graph paper and draw a straight line]

From the graph:

- (i) Line meets X-axis at **(4, 0)**
- (ii) Line meets Y-axis at **(0, 3)**
- (iii) One more point on the line: **(-4, 6)** or any other point satisfying the equation

MATH LOVE INSTITUTE - SOLUTIONS

SECTION E - SOLUTIONS (4 × 3 = 12 Marks)

Q36. Solution: CASE STUDY 1 - School Garden

Marking Scheme: 1 + 2 + 1 = 4 marks

(i) Semi-perimeter:

Sides: $a = 26$ m, $b = 28$ m, $c = 30$ m

$$s = (a + b + c)/2 = (26 + 28 + 30)/2 = 84/2$$

$$s = 42 \text{ m}$$

(ii) Area using Heron's formula:

$$\text{Area} = \sqrt{[s(s-a)(s-b)(s-c)]}$$

$$= \sqrt{[42(42-26)(42-28)(42-30)]}$$

$$= \sqrt{[42 \times 16 \times 14 \times 12]}$$

$$= \sqrt{[112896]}$$

$$= 336 \text{ m}^2$$

$$\text{Area} = 336 \text{ m}^2$$

(iii) Total cost:

Cost of planting grass = ₹15 per m^2

Total cost = Area × Rate

$$= 336 \times 15$$

$$= \text{₹}5040$$

Q37. Solution: CASE STUDY 2 - Water Tank

Marking Scheme: 1 + 1 + 2 = 4 marks

(i) Volume of large tank:

Radius = 1.4 m, Height = 2 m

$$\text{Volume} = \pi r^2 h$$

$$= (22/7) \times (1.4)^2 \times 2$$

$$= (22/7) \times 1.96 \times 2$$

$$= (22/7) \times 3.92$$

$$= 12.32 \text{ m}^3$$

Volume = 12.32 m³

(ii) Volume of small container:

Radius = 0.7 m, Height = 0.5 m

$$\text{Volume} = \pi r^2 h$$

$$= (22/7) \times (0.7)^2 \times 0.5$$

$$= (22/7) \times 0.49 \times 0.5$$

$$= (22/7) \times 0.245$$

$$= 0.77 \text{ m}^3$$

Volume = 0.77 m³

(iii) Number of containers required:

Number = Volume of large tank / Volume of one container

$$= 12.32 / 0.77$$

$$= 16$$

16 containers are required

Q38. Solution: CASE STUDY 3 - Temperature Analysis

Marking Scheme: 1 + 1 + 2 = 4 marks

(i) Class width:

Class width = Upper limit - Lower limit

Taking class 25-30: 30 - 25 = 5

Class width = 5°C

(ii) Class mark of 35-40:

$$\text{Class mark} = (\text{Lower limit} + \text{Upper limit})/2$$

$$= (35 + 40)/2$$

$$= 75/2$$

$$= 37.5^\circ\text{C}$$

(iii) Mean temperature:

Class	f_i	x_i	$f_i x_i$
25-30	4	27.5	110
30-35	8	32.5	260
35-40	12	37.5	450
40-45	6	42.5	255
Total	30	-	1075

$$\text{Mean} = \frac{\Sigma(f_i x_i)}{\Sigma f_i}$$

$$= 1075 / 30$$

$$= 35.83^\circ\text{C} \text{ (approximately } 35.8^\circ\text{C or } 36^\circ\text{C)}$$

© 2025 MATH LOVE INSTITUTE - SOLUTIONS

✓ END OF SOLUTIONS ✓

All solutions strictly based on CBSE Class 9 Syllabus 2025-26

Comprehensive step-by-step explanations with marking schemes

Key Topics Covered:

- Number Systems (Irrational Numbers, Rationalization)
- Polynomials (Factorization, Identities)
- Linear Equations in Two Variables
- Coordinate Geometry
- Triangles (Congruence, Angle Properties)
- Quadrilaterals

- Circles (Chord Properties)
 - Heron's Formula
- Surface Areas and Volumes
- Statistics (Mean, Mode, Frequency Distribution)

© 2025 Math Love Institute - Raipur, Chhattisgarh
For queries: www.mathloveinstitute.com

MATH LOVE INSTITUTE
© 2025 -
CONFIDENTIAL